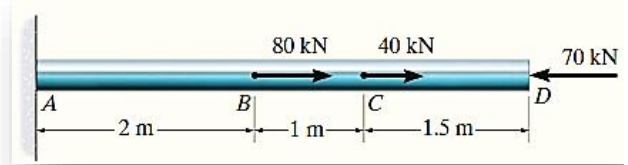


## ME212 Strength of Materials

### Chapter 4- Examples

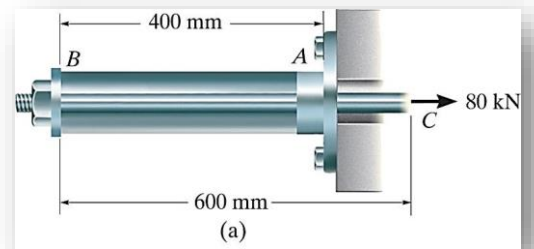
#### Exp. 1

The uniform A-36 steel bar in the Figure has a diameter of 50 mm and is subjected to the loading shown. Determine the displacement at  $D$ , and the displacement of point  $B$  relative to  $C$ . Take  $E_{A-36} = 200 \text{ GPa}$ .



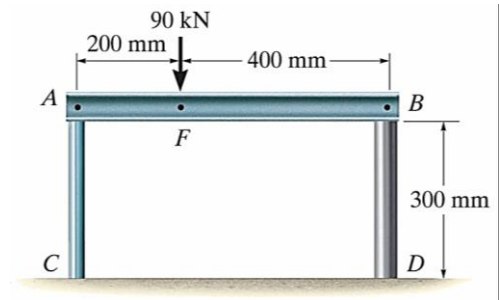
**Exp. 2**

The assembly shown in Figure(a) consists of an aluminum tube AB having a cross-sectional area of  $400 \text{ mm}^2$ . A steel rod having a diameter of  $10 \text{ mm}$  is attached to a rigid collar and passes through the tube. If a tensile load of  $80 \text{ kN}$  is applied to the rod, determine the displacement of end C of the rod. Take  $E_{\text{st}} = 200 \text{ GPa}$ ,  $E_{\text{al}} = 70 \text{ GPa}$



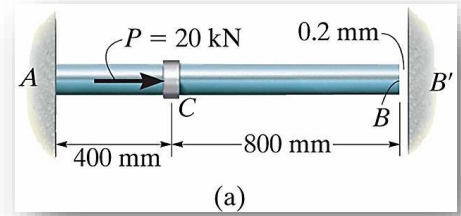
**Exp.3**

Rigid beam  $AB$  rests on the two short posts shown in the figure.  $AC$  is made of steel and has a diameter of 20 mm, and  $BD$  is made of aluminum and has a diameter of 40 mm. Determine the displacement of point  $F$  on  $AB$  if a vertical load of 90 kN is applied over this point. Take  $E_{st} = 200 \text{ GPa}$ ,  $E_{al} = 70 \text{ GPa}$



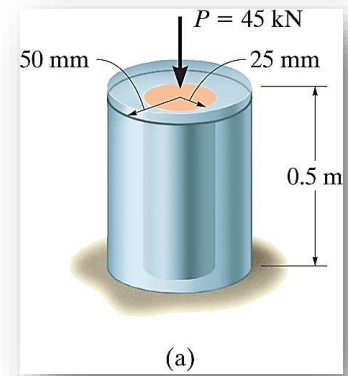
**Exp.4**

The steel rod shown in figure has a diameter of 10 mm. It is fixed to the wall at  $A$ , and before it is loaded, there is a gap of 0.2 mm between the wall at  $B'$  and the rod. Determine the reactions at  $A$  and  $B'$  if the rod is subjected to an axial force of  $P = 20$  kN as shown. Neglect the size of the collar at  $C$ . Take  $E_{\text{st}} = 200$  GPa.



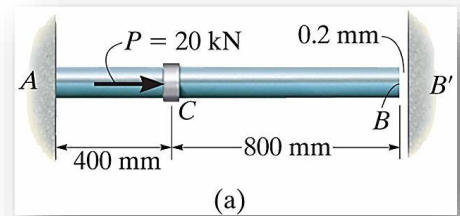
**Exp.5**

The aluminum post shown in Figure(a) is reinforced with a brass core. If this assembly supports an axial compressive load of  $P = 45$  kN, applied to the rigid cap, determine the average normal stress in the aluminum and the brass. Take  $E_{al} = 70(10^3)$  MPa and  $E_{br} = 105(10^3)$  MPa.



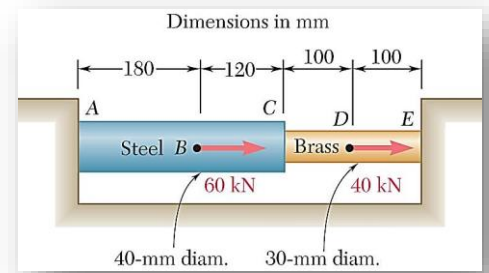
**Exp.6 (Exp 4-The Force Method)**

The steel rod shown in figure has a diameter of 10 mm. It is fixed to the wall at  $A$ , and before it is loaded, there is a gap of 0.2 mm between the wall at  $B'$  and the rod. Determine the reactions at  $A$  and  $B'$  if the rod is subjected to an axial force of  $P = 20$  kN as shown. Neglect the size of the collar at  $C$ . Take  $E_{st} = 200$  GPa.



**Exp.7**

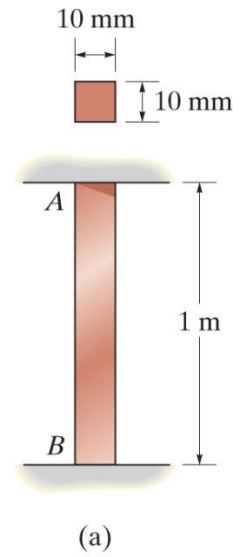
Two cylindrical rods, one of steel and the other of brass, are joined at  $C$  and restrained by rigid supports at  $A$  and  $E$ . For the loading shown and knowing that  $E_{st} = 200$  GPa and  $E_{br} = 105$  GPa, determine (a) the reactions at  $A$  and  $E$ , (b) the deflection of point  $C$ .



**Exp. 8**

The A-36 steel bar shown in Fig.(a) is constrained to just fit between two fixed supports when  $T_1 = 30^\circ\text{C}$ . If the temperature is raised to  $T_2 = 60^\circ\text{C}$ , determine the average normal thermal stress developed in the bar.

$$\alpha = 12(10^{-6})/^{\circ}\text{C}$$

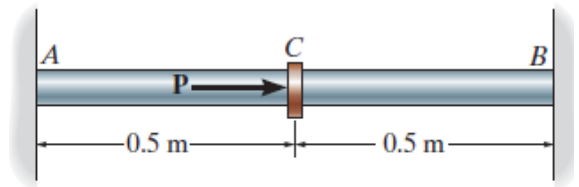




**Exp. 9**

The A-36 steel rod has a diameter of 50 mm and is lightly attached to the rigid supports at A and B when  $T_1 = 80^\circ\text{C}$ . If the temperature becomes  $T_2 = 20^\circ\text{C}$  and an axial force of  $P = 200\text{ kN}$  is applied to its center, determine the reactions at A and B.

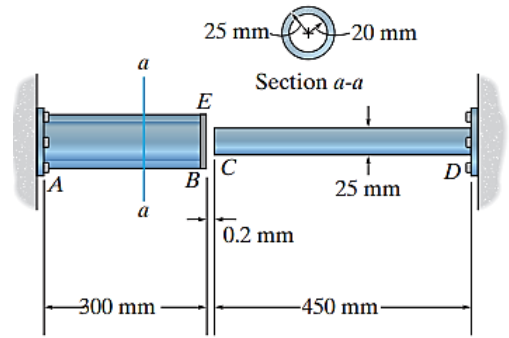
$$E_{st} = 200\text{ GPa}, \alpha = 12(10^{-6})/^\circ\text{C}$$



**Exp.10**

The AM1004-T61 magnesium alloy tube  $AB$  is capped with a rigid plate  $E$ . The gap between  $E$  and end  $C$  of the 6061-T6 aluminum alloy solid circular rod  $CD$  is 0.2 mm when the temperature is at  $30^\circ\text{C}$ . Determine the normal stress developed in the tube and the rod if the temperature rises to  $80^\circ\text{C}$ . Neglect the thickness of the rigid cap.

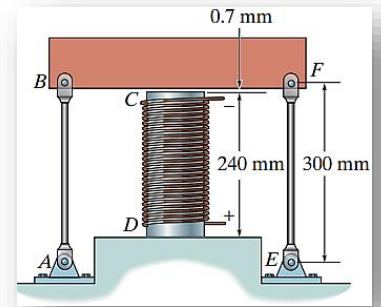
$$\alpha_{mg} = 26(10^{-6})/^\circ\text{C}, \quad \alpha_{al} = 24(10^{-6})/^\circ\text{C},$$
$$E_{mg} = 44.7 \text{ GPa}, \quad E_{al} = 68.9 \text{ GPa},$$



**Exp.11**

The center rod  $CD$  of the assembly is heated from  $T_1 = 30^\circ\text{C}$  to  $T_2 = 180^\circ\text{C}$  using electrical resistance heating. At the lower temperature  $T_1$  the gap between  $C$  and the rigid bar is  $0.7\text{ mm}$ . Determine the force in rods  $AB$  and  $EF$  caused by the increase in temperature. Rods  $AB$  and  $EF$  are made of steel, and each has cross-sectional area of  $125\text{ mm}^2$ .  $CD$  is made of aluminum, and has cross-sectional area of  $375\text{ mm}^2$ .

$E_{st} = 200\text{ GPa}$ ,  $E_{al} = 70\text{ GPa}$  and  $\delta_{al} = 23(10^{-6})/^\circ\text{C}$



**Exp.12**

The rigid link is supported by a pin at A, a steel wire  $BC$  having an unstretched length of 200 mm and cross-sectional area of  $22.5 \text{ mm}^2$  and a short aluminum block having an unloaded length of 50 mm and cross-sectional area of  $40 \text{ mm}^2$ . If the link is subjected to the vertical load shown, determine the average normal stress in the wire and the block.  $E_{st} = 200 \text{ GPa}$ ,  $E_{al} = 70 \text{ GPa}$ .

